

CALIFORNIA INSTITUTE OF TECHNOLOGY  
Control and Dynamical Systems

**CDS 110b**

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**Problem Set #1**

Issued: 9 Jan  
Due: 16 Jan, 4 pm

1. Consider the inverted pendulum dynamics as described in equation 1 in the posted class notes. Linearize the dynamics about both the up and down equilibria and design stabilizing controllers for  $\tau = 0$ ,  $l = 1$  and different lengths  $l_0$ , using **only** the techniques from CDS 110a. Let  $l_0 = 1$ ,  $l_0 = 0.75$ ,  $l_0 = 0.5$  and the smallest  $l_0$  you can come up with a stabilizing controller for. For each controller design, hand in a pole-zero plot and Bode plots and comment on gain and phase margins.